In the name of God

## Department of Physics Shahid Beheshti University

## ADVANCED STATISTICAL MECHANICS I

## Exercise Set 2

(Due Date: 1400/09/06)

1. Zero law of thermodynamics: suppose that A, B and C are in thermal equilibrium. For A and C, we have:

$$P_A V_A - n_A r_A P_A - P_C V_C = 0$$

and for B and C, we have:

$$P_B V_B - P_C V_C + \frac{n_B r_B P_C V_C}{V_B} = 0$$

Find 3 state equations of this system which are in thermal equilibrium.

2. Show that the violation of Kelvin-Planck's statement yields the violation of Clausius's statement and vise versa.

3. Show that it is impossible to have an engine possessing efficiency higher than Carnot engine.

**4.** Suppose that a system with  $T_s$  is contacted thermally with a reservoir with  $T_R$ .

**A**: Compute  $\Delta S_{total} = \Delta S_{reservoir} + \Delta S_{system}$  if at the initial point  $T_R > T_s$ .

**B**: Compute  $\Delta S_{total} = \Delta S_{reservoir} + \Delta S_{system}$  if at the initial point  $T_R < T_s$ .

C: For each cases, plot the  $\Delta S_{total}$ ,  $\Delta S_{reservoir}$  and  $\Delta S_{system}$  as a function of  $T_R/T_s$ 

5. Producing a piece of ice during a night at desert. Is it possible to freeze water in a plate in the naked sky in desert? (Hint; suppose that the temperature of water is T = 6°C and the temperature of naked dark sky is T = -23°C. The time for doing experiment would be sunset till sunrise.)

**6.** We have a refrigerator which its power equates to 100W and a heater with 100W are working in the room temperature. Which system makes more heat in the room. Explain your answer.

7. We have a box isolated from the environment with volume V. We divided it into two parts with xV and (1-x)V. Pressures and temperatures in both partition are equal. There are xn and (1-x)n particle in left and right parts, respectively. Now we remove the partition, how much changes will be occurred in Entropy?

Good luck, Movahed